

Gravitational collapse: confined geometries



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Cosmic Censorship

Horizon formation

Spacetime stability

DEMETRIOS CHRISTODOULOU
SERGIU KLAINERMAN

The Global
Nonlinear Stability
of the Minkowski
Space (PMS-41)

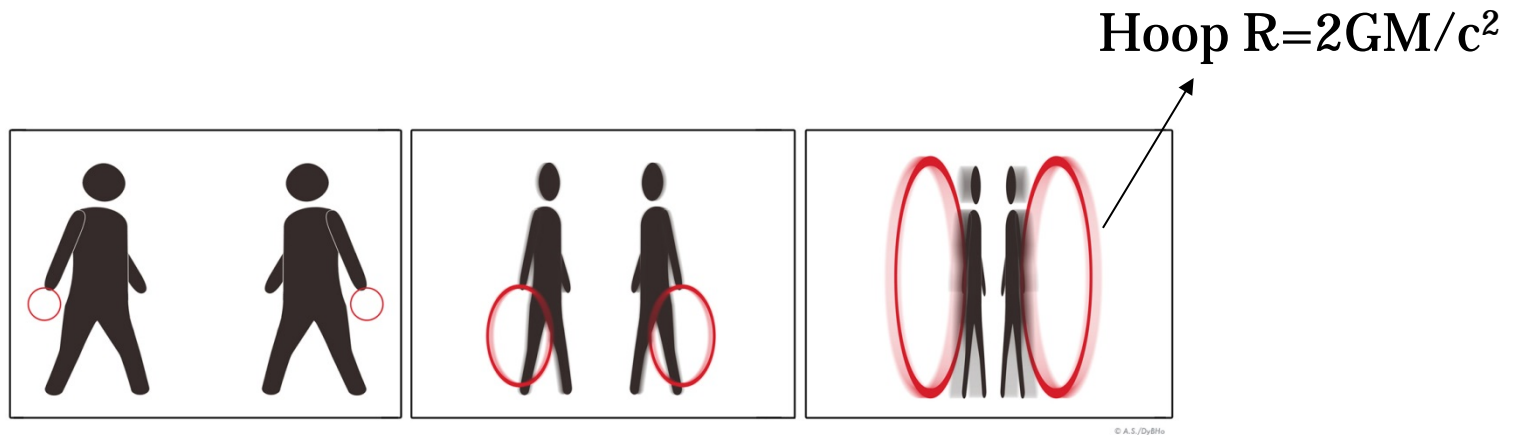
 PRINCETON LEGACY LIBRARY

Hoop Conjecture

(Thorne 1972)

“An imploding object forms a BH when, and only when, a circular hoop with circumference 2π the Schwarzschild radius of the object can be made that encloses the object in all directions.”

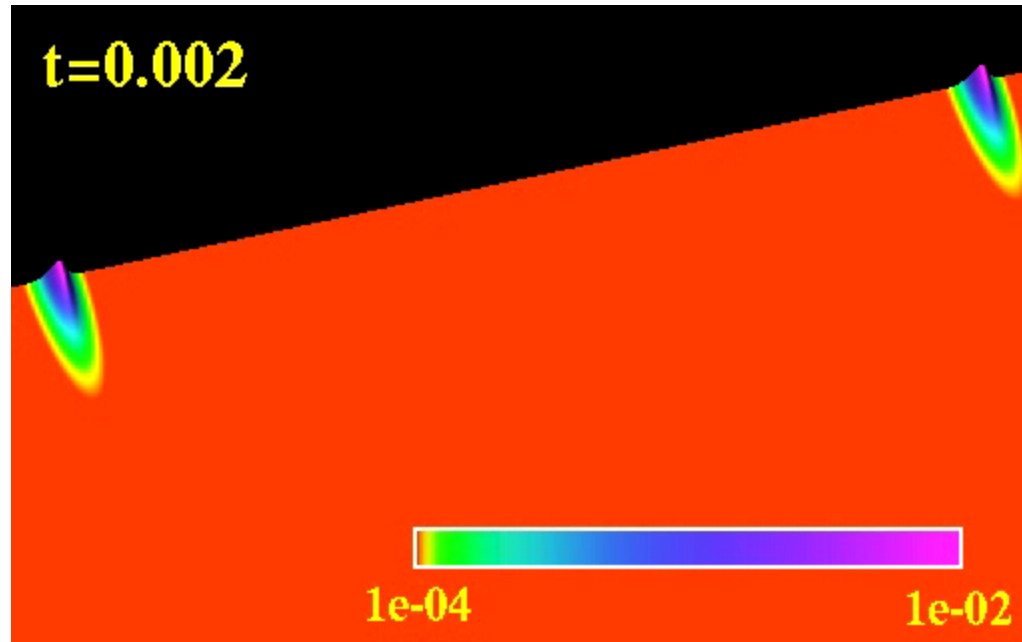
Large amount of energy in small region



Size of electron: 10^{-17} cm

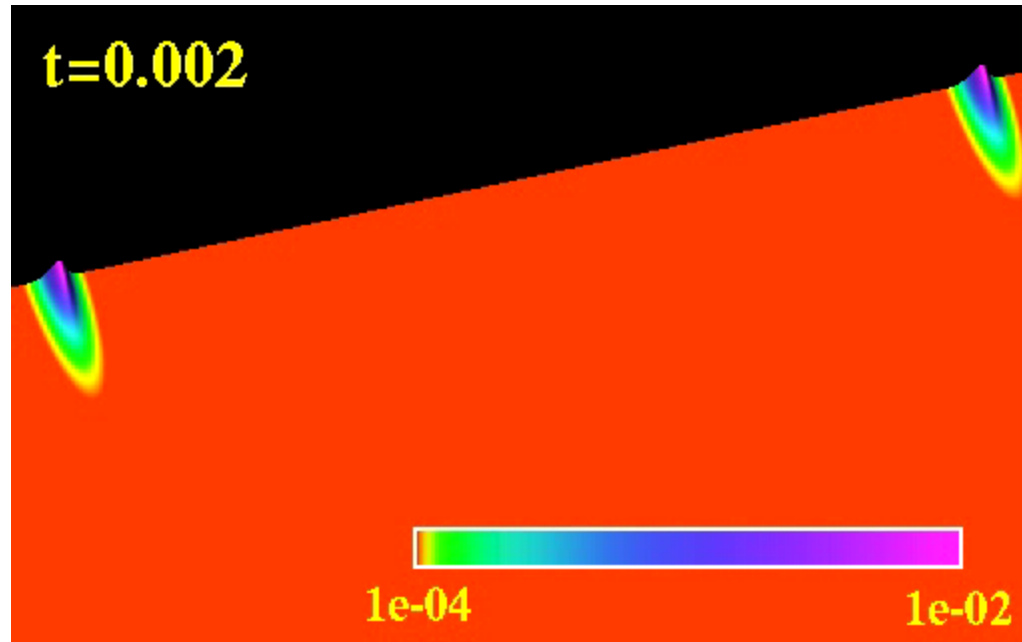
Schwarzschild radius: 10^{-55} cm

$$2M/R = 1/20 \implies \gamma_{\text{crit}} \sim 10$$

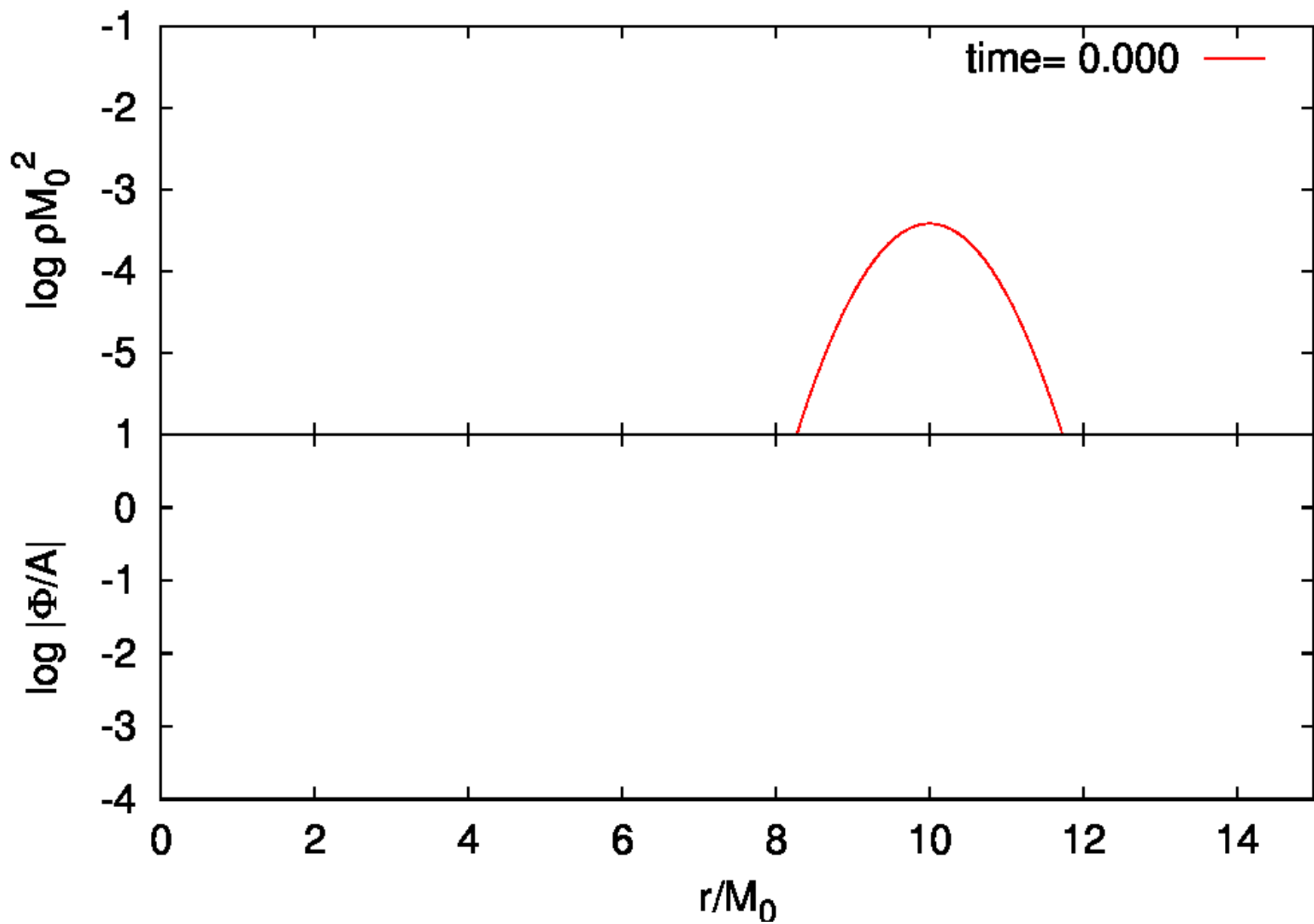


(Choptuik & Pretorius 2010, East & Pretorius 2012, Rezzolla & Takami 2012)

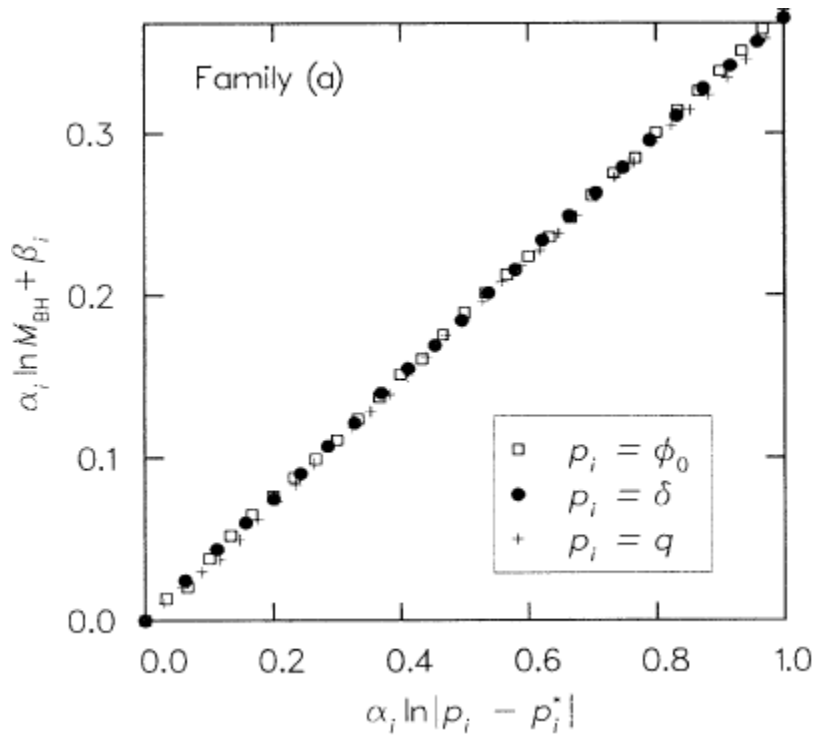
$$2M/R = 1/20 \implies \gamma_{\text{crit}} \sim 10$$



(Choptuik & Pretorius 2010, East & Pretorius 2012, Rezzolla & Takami 2012)



Collapse of massless scalar fields



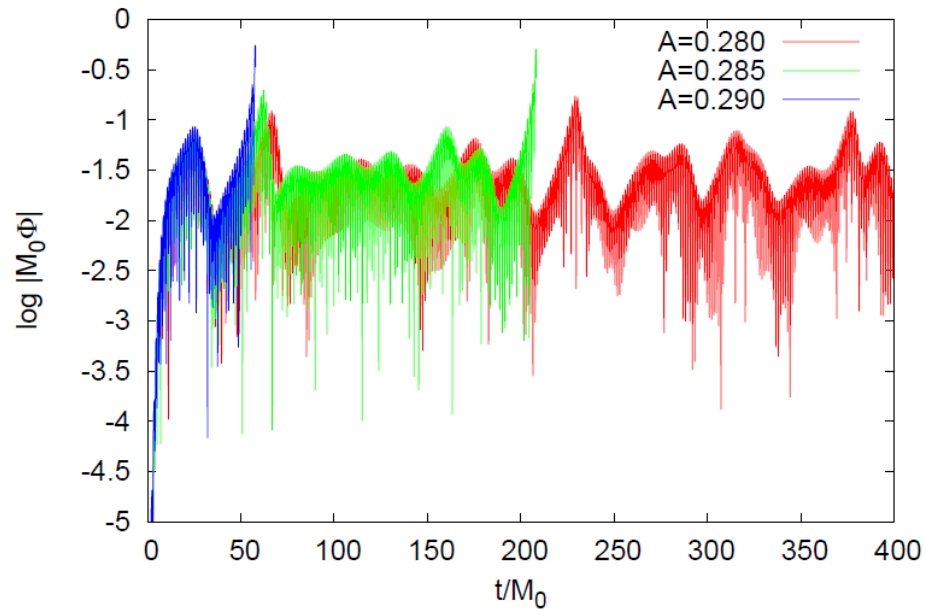
$$\phi = \phi_0 r^3 \exp\left(-[(r - r_0)/\delta]^q\right)$$

$$M \propto (p - p_*)^\gamma$$

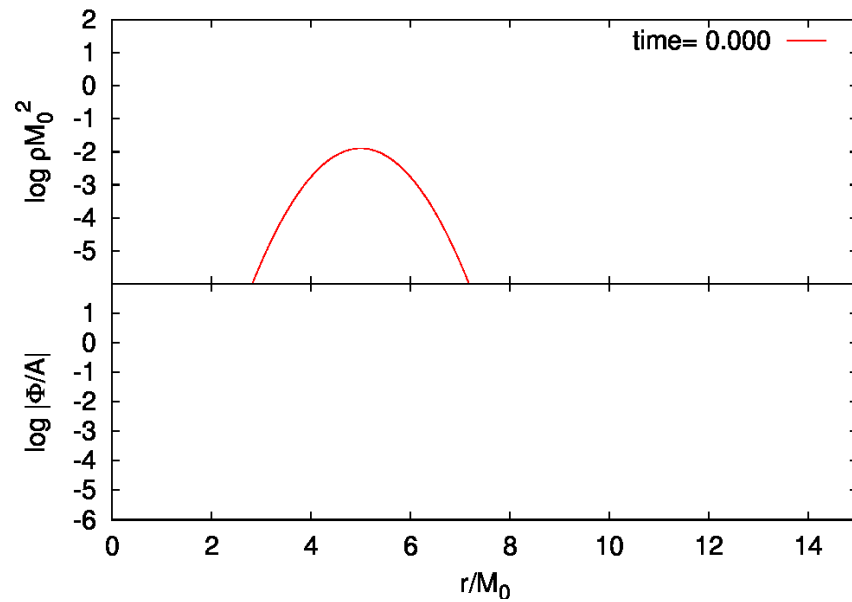
Confined geometries

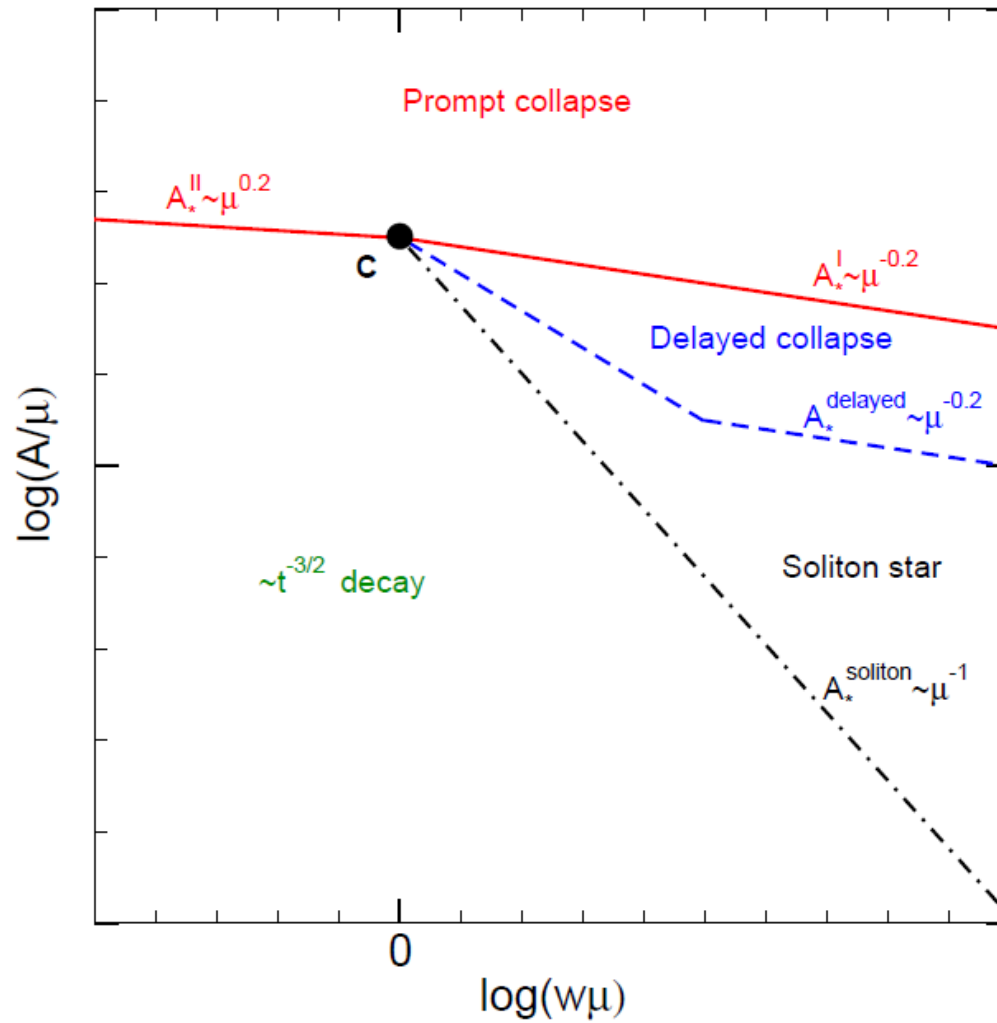
Expect generically to favour collapse

Important for some realistic setups: stars, massive fields, AdS



$r_0 = 5, w = 1.25$ and $\mu = 2$





Collapse in anti-de Sitter

Maximally symmetric manifold, with constant negative scalar curvature

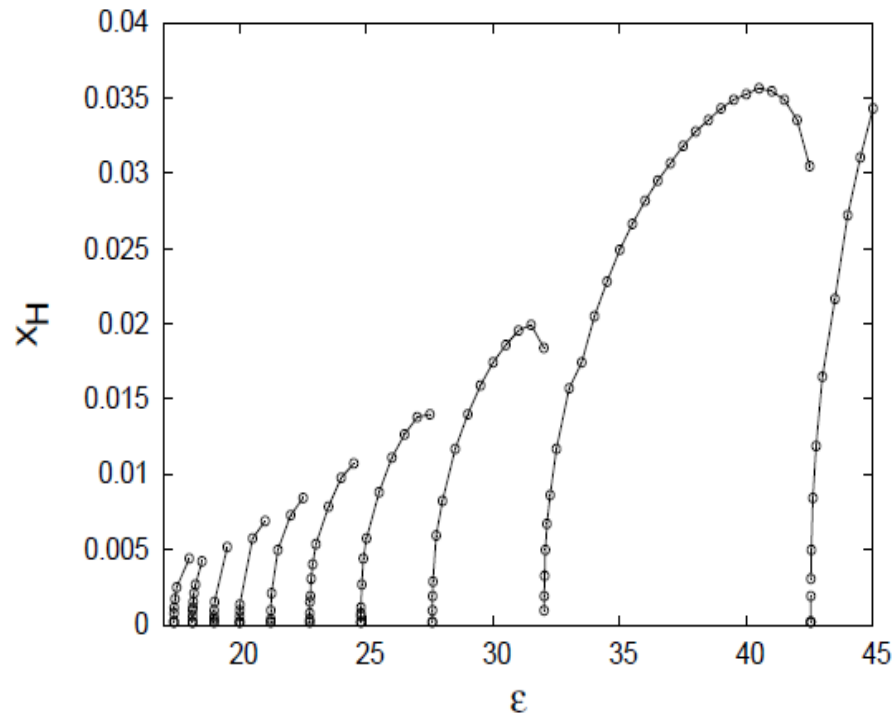
(the Lorentzian analogue of an hyperboloid)



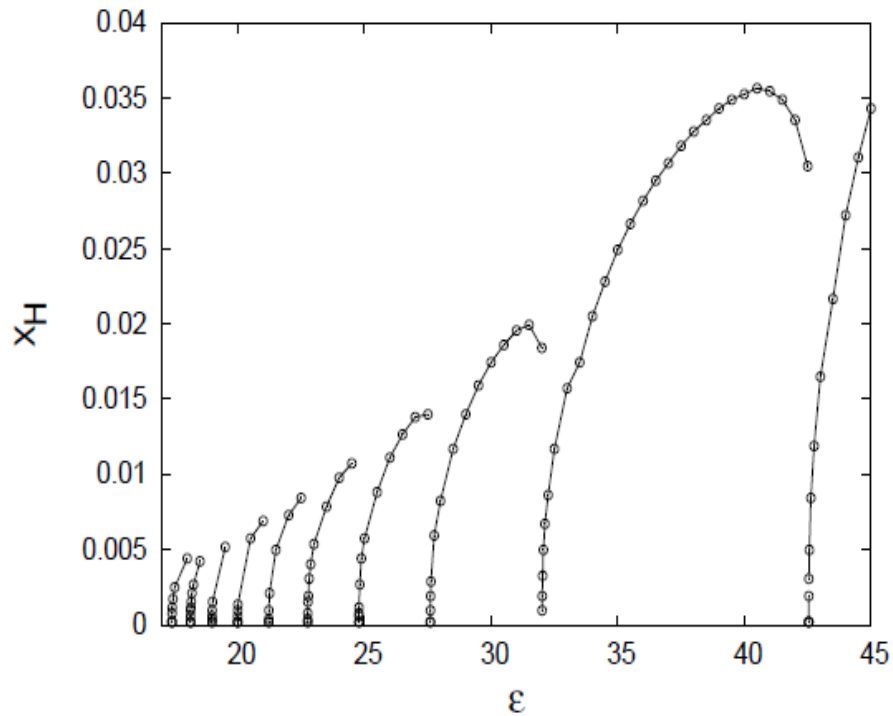
$$ds^2 = -(r^2/L^2 + 1)dt^2 + \frac{dr^2}{r^2/L^2 + 1} + r^2 d\Omega^2$$

$$dr/dt = r^2/L^2 + 1, \quad t_{\text{travel}} = \pi L/2$$

Collapse in anti-de Sitter



Collapse in anti-de Sitter



...AdS is nonlinearly unstable!

Resonances?

$$G_{\mu\nu} + \Lambda g_{\mu\nu} = 8\pi G \left(\partial_\mu \phi \partial_\nu \phi - \frac{1}{2} g_{\mu\nu} (\partial\phi)^2 \right)$$

$$\square\phi = 0$$

$$ds^2 = \frac{\ell^2}{\cos^2 x} \left(-Ae^{-2\delta} dt^2 + A^{-1} dx^2 + \sin^2 x d\Omega^2 \right)$$

$$\phi(t, x) = \sum_{j=0}^{\infty} \phi_{2j+1} \epsilon^{2j+1}, \quad A = 1 - \sum_{j=1}^{\infty} A_{2j} \epsilon^{2j}, \quad \delta = \sum_{j=1}^{\infty} \delta_{2j} \epsilon^{2j}$$

$$\phi_1(t, x) = \sum_{j=0}^{\infty} a_j \cos(\omega_j t + \beta_j) e_j(x)$$

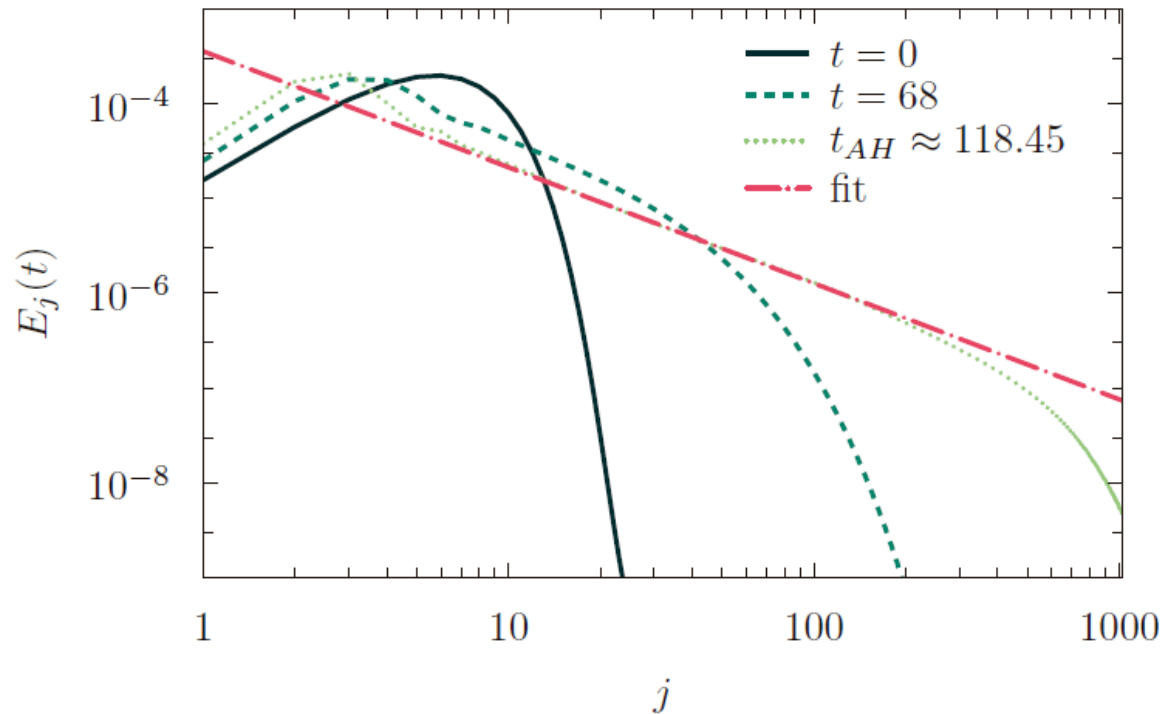
$$\ddot{\phi}_3 + L\phi_3 = S(\phi_1, A_2, \delta_2)$$

Resonances appear whenever

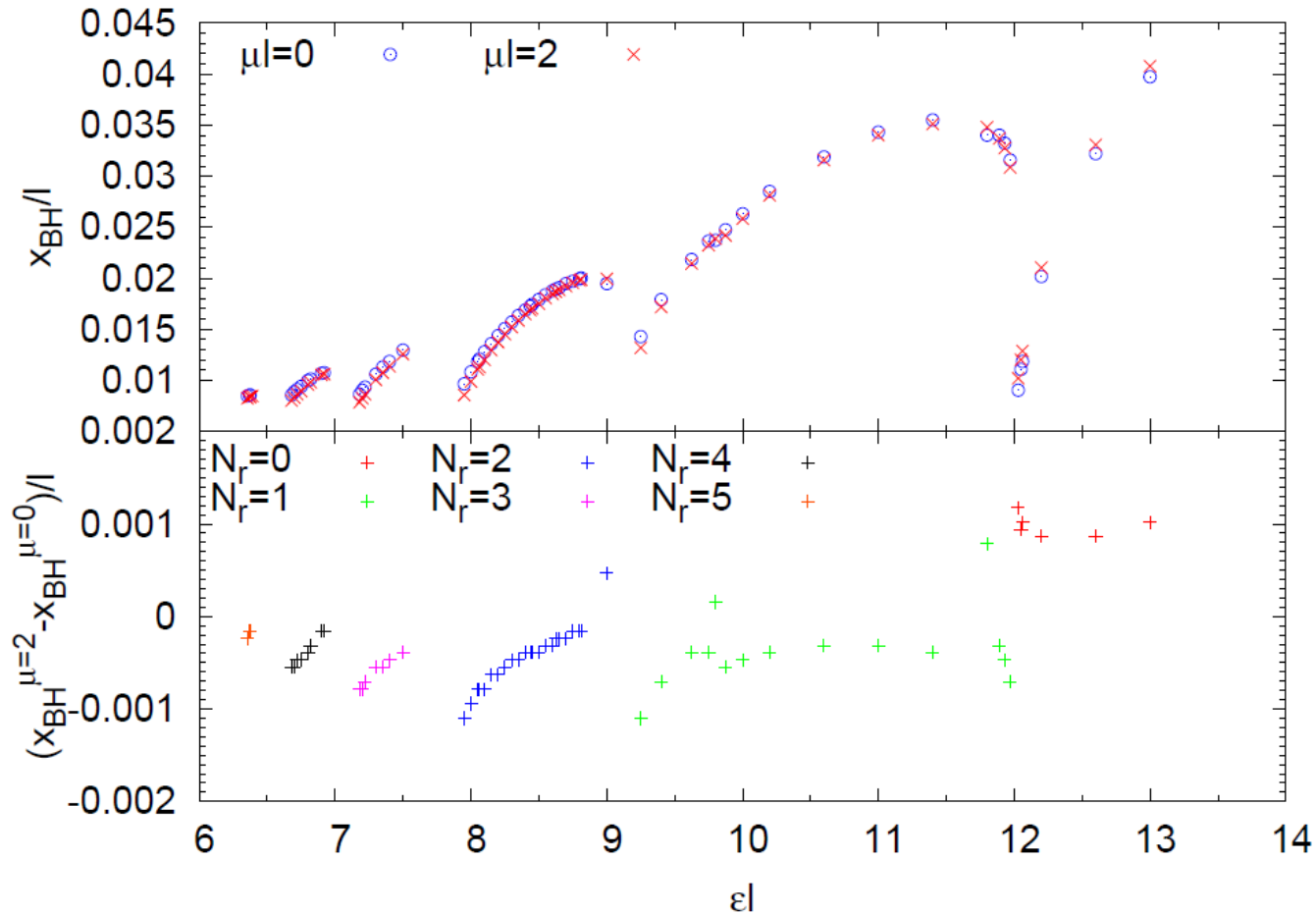
$$\omega_j = \omega_{j_1} + \omega_{j_2} - \omega_{j_3}$$

Weak turbulence?

Resonances appear whenever $\omega_j = \omega_{j_1} + \omega_{j_2} - \omega_{j_3}$

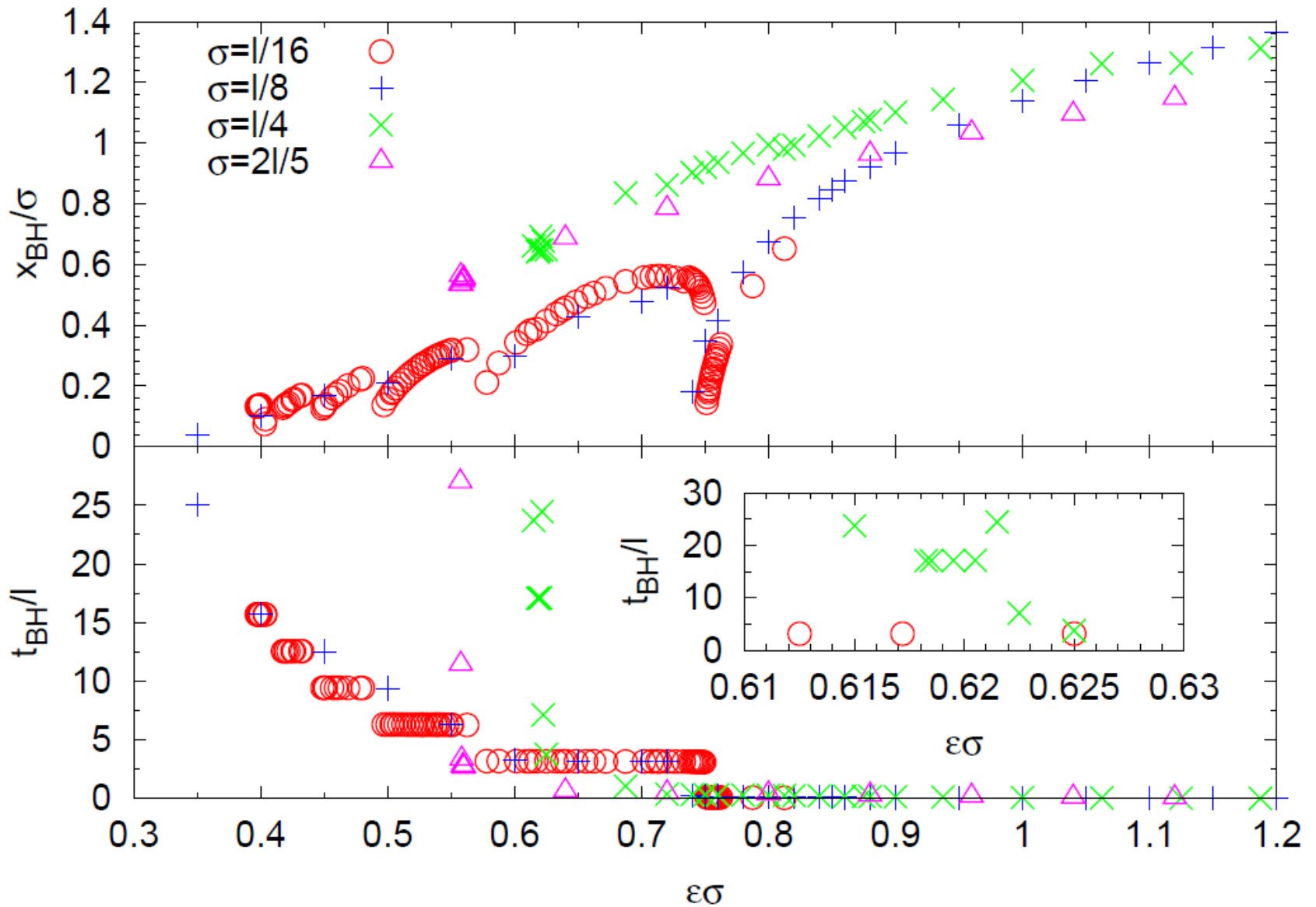


Massive fields?

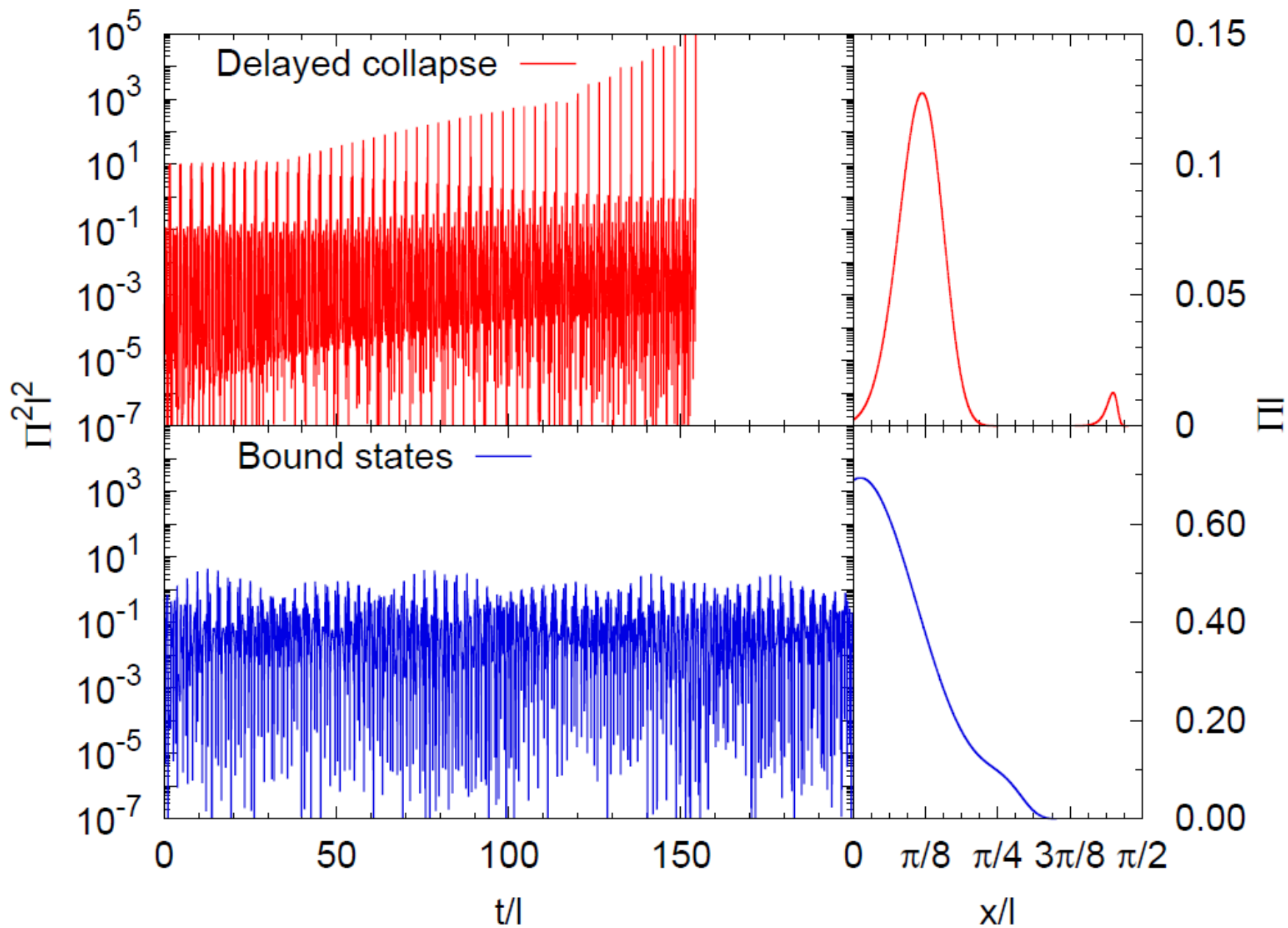


Resonances suggest that massive fields should also be turbulent...checked!

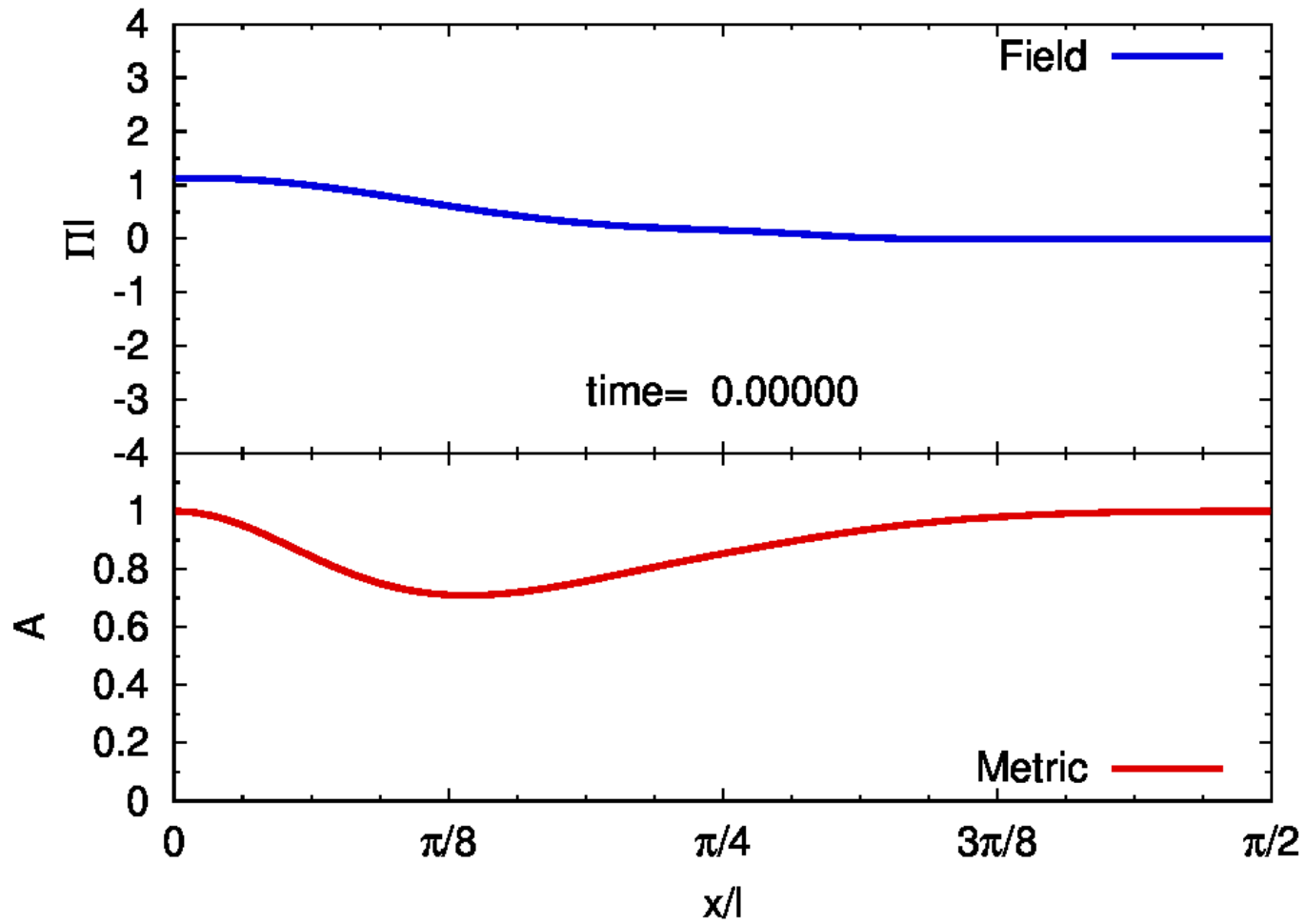
Okawa, Lopes & Cardoso 2015

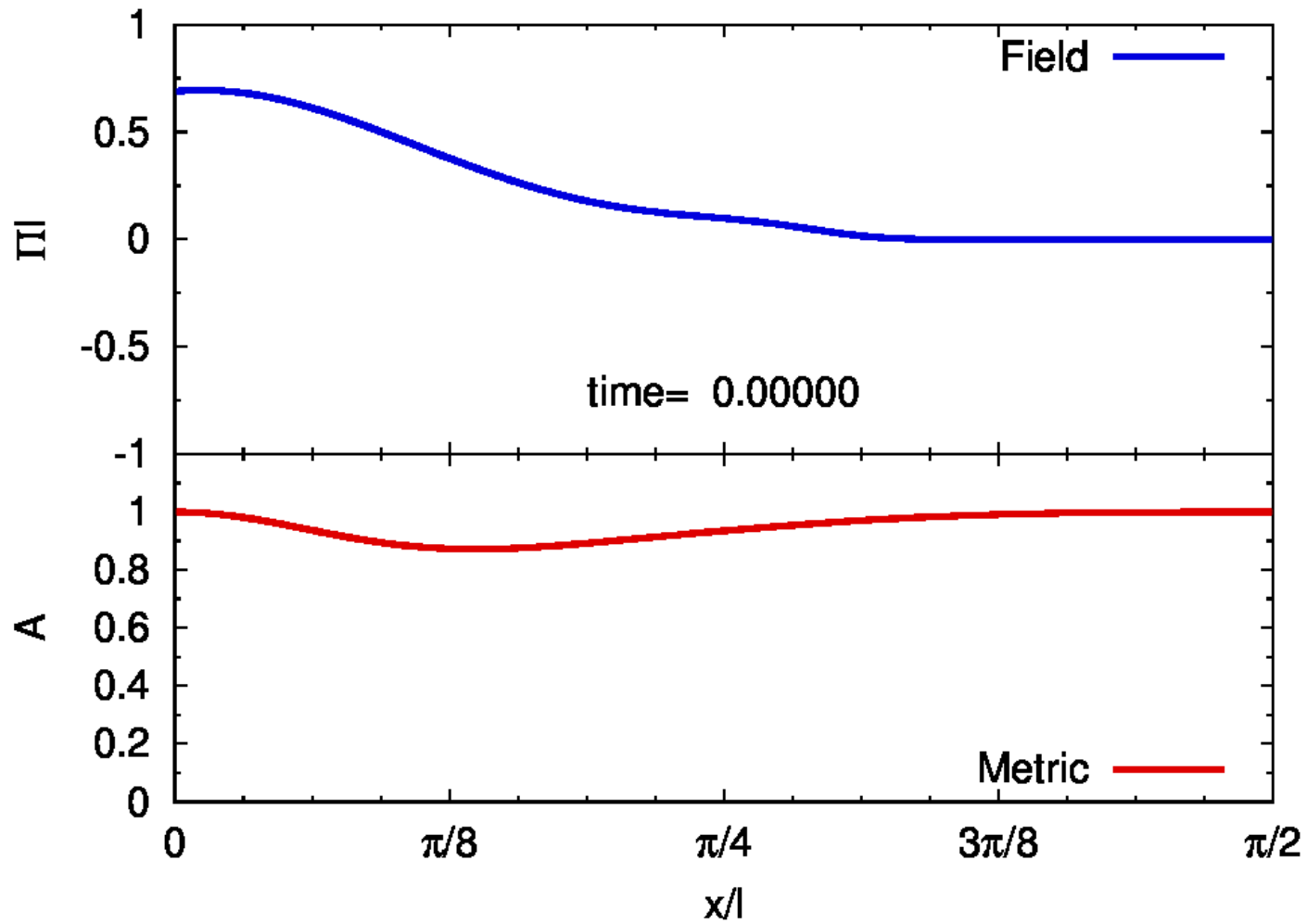


Wide initial data does not collapse...similar to oscillons of massive fields?...



Three wavepackets: collapse





Strong field gravity is a fascinating topic

Collapse close to critical points is of a self-similar nature and leads to a naked singularity (while not violating cosmic censorship in spirit). Collapse in confined geometries either forms nonlinearly-stable structures, or collapses at arbitrarily-small amplitudes.

Delayed collapse of small amplitude fields remains a mystery. There are consequences for the gauge-gravity duality (essential thermalization of any field theory), are there consequences for astrophysics? Consequences for stability of stars?

Thank you

